MAT229 Quiz 09, Spring 2025

Name:

1. (4 pts) Use a comparison test to determine whether the following series converge or diverge. (Do not use the Integral test!)

a.
$$\sum_{n=1}^{\infty} \frac{1}{(n \ln(n))^2}$$

b.
$$\sum_{n=1}^{\infty} \frac{e^n}{1 + e^{2n}}$$

2. (2 pts) Use limit comparison to decide the convergence of $\sum_{n=1}^{\infty} \frac{\ln(1+\frac{1}{n})}{n}$ (try a p-series).

3. (4 pts) For the following series, find the value of n such that it converges to within 0.0001 of its limit.

a.
$$\sum_{n=1}^{\infty} (-1)^{n+1} \frac{1}{n^2}$$

b.
$$\sum_{n=2}^{\infty} (-1)^{n+1} \frac{1}{\ln(n)}$$