

#1

$$f(x) = \frac{\sin x}{x^2}$$

$$f'(x) = \frac{x^2 \cos x - 2x \sin x}{x^4}$$

#2

$$f(x) = \sec(1+x^2)$$

$$f'(x) = \sec(1+x^2) \tan(1+x^2) 2x$$

#3

$$f(x) = (x^2 - x + 1)^3$$

$$f'(x) = 3(x^2 - x + 1)^2 (2x - 1)$$

#4

$$f(x) = (2x-5)^4 (8x^2-5)^{-3}$$

$$f'(x) = 4(2x-5)^3 (2) (8x^2-5)^{-3} + (-3)(8x^2-5)^{-4} (16x) (2x-5)^4$$

#5

$$f(x) = \frac{(x-1)^4}{(x^2+5x)^5}$$

$$f'(x) = \frac{(x^2+5x)^5 4(x-1)^3 - (x-1)^4 5(x^2+5x)^4 (2x+5)}{(x^2+5x)^{10}}$$

#6

$$f(x) = \sin(x \cos x)$$

$$f'(x) = \cos(x \cos x) (-x \sin x + \cos x)$$

#7

$$1 + x = \sin(xy^2)$$

$$1 = \cos(xy^2) (x \cdot 2y y' + y^2)$$

$$1 = 2xy \cos(xy^2) y' + y^2 \cos(xy^2)$$

$$1 - y^2 \cos(xy^2) = 2xy \cos(xy^2) y'$$

$$y' = \frac{1 - y^2 \cos(xy^2)}{2xy \cos(xy^2)}$$

#8

$$y = \sqrt{x^2 + 1} = (x^2 + 1)^{1/2}$$

$$y' = \frac{1}{2} (x^2 + 1)^{-1/2} \cdot 2x$$

$$= x (x^2 + 1)^{-1/2}$$

$$y'' = x \left(-\frac{1}{2}\right) (x^2 + 1)^{-3/2} (2x)$$

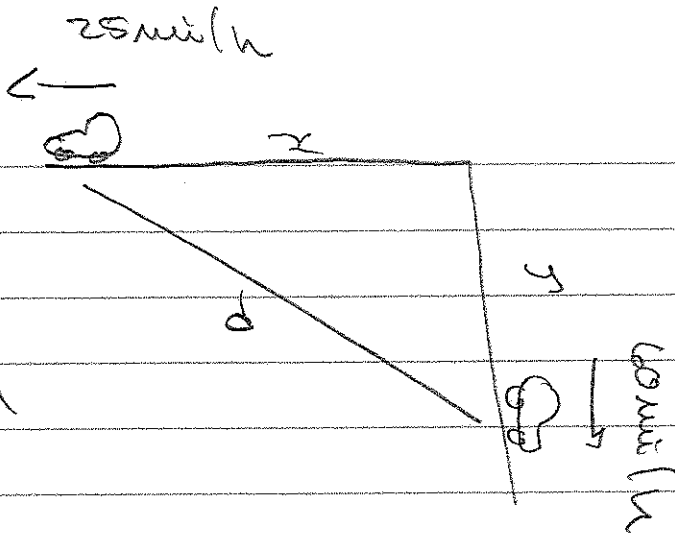
$$+ (x^2 + 1)^{-1/2}$$

#9

$$\frac{dx}{dt} = 25 \text{ mi/h}$$

$$\frac{dy}{dt} = 60 \text{ mi/h}$$

$$\frac{dd}{dt} = ?$$



$$d^2 = x^2 + y^2$$
$$2d \frac{dd}{dt} = 2x \frac{dx}{dt} + 2y \frac{dy}{dt}$$

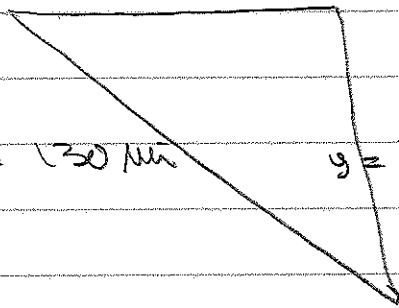
$$\frac{dd}{dt} = \frac{x}{d} \frac{dx}{dt} + \frac{y}{d} \frac{dy}{dt}$$

after 2 hours

$$x = 50 \text{ mi}$$

$$d = 130 \text{ mi}$$

$$y = 120 \text{ mi}$$



$$\frac{dd}{dt} = \frac{50 \text{ mi}}{130 \text{ mi}} (25 \text{ mi/h}) + \frac{120 \text{ mi}}{130 \text{ mi}} (60 \text{ mi/h})$$
$$= 65 \text{ mi/h}$$